

# Package ‘wINEQ’

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**Title** Inequality Measures for Weighted Data

**Version** 1.2.0

**Description** Computes inequality measures of a given variable taking into account weights. Bootstrap method provides distribution of inequality measures and several additional statistics.

**License** GPL-3

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AF	<i>Allison and Foster index</i>
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### Description

Computes Allison and Foster inequality measure of a given variable taking into account weights.

### Usage

```
AF(X, W = rep(1, length(X)), norm = TRUE)
```

### Arguments

X	is a data vector (numeric or ordered factor)
W	is a vector of weights
norm	(logical). If TRUE (default) then index is divided by a maximum possible value which is a difference between maximum and minimum of X

### Details

Let  $c = (c_1, \dots, c_n)$  be the vector of categories in increasing order,  $m$  be the median category and  $p_i$  be a share of  $i$ -th category. The following index was proposed by Allison and Foster (2004):

$$AF = \frac{\sum_{i=m}^n c_i p_i}{\sum_{i=m}^n p_i} - \frac{\sum_{i=1}^{m-1} c_i p_i}{\sum_{i=1}^{m-1} p_i}$$

Note that above formula is valid only for numerical values. Thus, in order to compute AF for ordered factor, X is converted to numerical variable.

### Value

The value of Allison and Foster coefficient.

## References

Allison R. A., Foster J E.: (2004) Measuring health inequality using qualitative data, Journal of Health Economics

## Examples

```
# Compare weighted and unweighted result
X=1:10
W=1:10
AF(X)
AF(X,W)

data(Well_being)
# Allison and Foster index for health assessment with sample weights
X=Well_being$V11
W=Well_being$Weight
AF(X,W)
```

---

 AN\_Y

*Abul Naga and Yalcin index*


---

## Description

Computes Abul Naga and Yalcin inequality measure of a given variable taking into account weights.

## Usage

```
AN_Y(X, W = rep(1, length(X)), a = 1, b = 1)
```

## Arguments

X	is a data vector (numeric or ordered factor)
W	is a vector of weights
a	is a positive parameter. See more in details
b	is a positive parameter. See more in details

## Details

Let  $m$  be the median category,  $n$  be the number of categories and  $P_i$  be the cumulative distribution of  $i$ -th category. The following index with respect to the parameters  $a$  and  $b$  was proposed by Abul Naga and Yalcin (2008):

$$I = \frac{a \sum_{i < m}^n P_i - b \sum_{i \geq m}^n P_i + b(n + 1 - m)}{0.5(a(m - 1) + b(n - m))}$$

**Value**

The value of Abul Naga and Yalcin coefficient.

**References**

Ramses H. Abul Naga and Tarik Yalcin: (2008) Inequality Measurement for ordered response health data, *Journal of Health Economics* 27(6);

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
AN_Y(X)
AN_Y(X,W)

data(Well_being)
# Abul Naga and Yalcin index for health assessment with sample weights
X=Well_being$V1
W=Well_being$Weight
AN_Y(X,W)
```

---

Apouey

*Apouey index*

---

**Description**

Computes Apouey inequality measure of a given variable taking into account weights.

**Usage**

```
Apouey(
  X,
  W = rep(1, length(X)),
  a = 2/(1 - length(W[!is.na(W) & !is.na(X)])),
  b = length(W[!is.na(W) & !is.na(X)])/(length(W[!is.na(W) & !is.na(X)] - 1)
)
```

**Arguments**

X is a data vector (numeric or ordered factor)  
 W is a vector of weights  
 a is a positive parameter. See more in details  
 b is a real parameter. See more in details

**Details**

Let  $m$  be the median category,  $n$  will be the number of categories and  $P_i$  be the cumulative distribution of  $i$ -th category. The following index was proposed by Apouey (2007):

$$I = \alpha \left( \sum_{i \geq m}^n P_i - \sum_{i < m}^n P_i + m - \frac{n}{2} - 1 \right) + \beta$$

where  $\alpha$  and  $\beta$  are given parameters with default values  $\alpha = \frac{2}{1-n}$  and  $\beta = \frac{n}{n-1}$ .

**Value**

The value of Apouey coefficient.

**References**

Apouey B.: (2007) Measuring health polarization with self-assessed health data, *Health Economics* 16; 875-894.

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Apouey(X,a=2,b=2)
Apouey(X,W,a=2,b=2)

data(Well_being)
# Apouey index for health assessment with sample weights
X=Well_being$V1
W=Well_being$Weight
Apouey(X,W,a=2,b=2)
```

---

 Atkinson

*Atkinson index*


---

**Description**

Computes Atkinson inequality measure of a given variable taking into account weights.

**Usage**

```
Atkinson(X, W = rep(1, length(X)), e = 1)
```

**Arguments**

X	is a data vector
W	is a vector of weights
e	is a coefficient of aversion to inequality, by default 1

**Details**

Atkinson coefficient with respect to parameter  $\epsilon$  is given by

$$1 - \frac{1}{\mu} \left( \frac{1}{n} \sum_{i=1}^n x_i^{1-\epsilon} \right)^{\frac{1}{1-\epsilon}}$$

for  $\epsilon \neq 1$  and

$$1 - \frac{1}{\mu} \left( \prod_{i=1}^n x_i \right)^{\frac{1}{n}}$$

for  $\epsilon = 1$ .

**Value**

The value of Atkinson coefficient.

**References**

Atkinson A. B.: (1970) On the measurement of inequality, Journal of Economic Theory

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Atkinson(X)
Atkinson(X,W)

data(Tourism)
# Atkinson index for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Atkinson(X,W)
```

---

 BL

*Blair and Lacy index*


---

**Description**

Computes Blair and Lacy inequality measure of a given variable taking into account weights.

**Usage**

```
BL(X, W = rep(1, length(X)), withsqrt = FALSE)
```

**Arguments**

X	is a data vector (numeric or ordered factor)
W	is a vector of weights
withsqrt	if TRUE function returns index given by BL2, elsewhere by BL (default). See more in details.

**Details**

Let  $m$  be the median category,  $n$  be the number of categories and  $P_i$  be the cumulative distribution of  $i$ -th category. The indices of Blair and Lacy (2000) are the following:

$$BL = 1 - \frac{\sum_{i=1}^{n-1} (P_i - 0.5)^2}{\frac{n-1}{4}}$$

$$BL2 = 1 - \left( \frac{\sum_{i=1}^{n-1} (P_i - 0.5)^2}{\frac{n-1}{4}} \right)^{\frac{1}{2}}$$

**Value**

The value of Blair and Lacy coefficient.

**References**

Blair J, Lacy M G. (2000): Statistics of ordinal variation, *Sociological Methods and Research* 28(251);251-280.

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
BL(X)
BL(X,W)

data(Well_being)
# Blair and Lacy index for health assessment with sample weights
X=Well_being$V1
W=Well_being$Weight
BL(X,W)
```

---

CoefVar	<i>Coefficient of Variation</i>
---------	---------------------------------

---

**Description**

Computes Coefficient of Variation inequality measure of a given variable taking into account weights.

**Usage**

```
CoefVar(X, W = rep(1, length(X)), square = FALSE)
```

**Arguments**

X	is a data vector	
W	is a vector of weights	
square	logical, argument of the function CoefVar, for details see below	

**Details**

Coefficient of variation is given by:

$$CV = \frac{\sigma}{\mu} \times 100$$

where  $\sigma$  is a standard deviation and  $\mu$  is arithmetic mean.

**Value**

The value of CoefVar coefficient.

**References**

Sheret M.: (1984) Social Indicators Research, An International and Interdisciplinary Journal for Quality-of-Life Measurement, Vol. 15, No. 3, Oct. ISSN 03038300  
 Coulter P. B.: (1989) Measuring Inequality ISBN 0-8133-7726-9

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
CoefVar(X)
CoefVar(X,W)

data(Tourism)
#Coefficient of variation for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
CoefVar(X,W)
```



Entropy

*Generalized entropy index***Description**

Computes generalized entropy index of a given variable taking into account weights.

**Usage**

```
Entropy(X, W = rep(1, length(X)), parameter = 0.5)
```

**Arguments**

X	is a data vector
W	is a vector of weights
parameter	is a entropy parameter

**Details**

Entropy coefficient with respect to parameter  $\alpha$  is equal to  $\text{Theil\_L}(X,W)$  whenever  $\alpha = 0$ , is equal to  $\text{Theil\_T}(X,W)$  whenever  $\alpha = 1$ , and whenever  $\alpha \in (0, 1)$  we have

$$GE(\alpha) = \frac{1}{\alpha(\alpha - 1)W} \sum_{i=1}^n w_i \left( \left( \frac{x_i}{\mu} \right)^\alpha - 1 \right)$$

where  $W$  is a sum of weights and  $\mu$  is the arithmetic mean of  $x_1, \dots, x_n$ .

**Value**

The value of generalized entropy index

**References**

Shorrocks A. F.: (1980) The Class of Additively Decomposable Inequality Measures. *Econometrica*  
 Pielou E.C.: (1966) The measurement of diversity in different types of biological collections. *Journal of Theoretical Biology*

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Entropy(X)
Entropy(X,W)

data(Tourism)
# Generalized entropy index for Total expenditure with sample weights
X=Tourism$`Total expenditure`
```

```
W=Tourism$`Sample weight`
Entropy(X,W)
```

---

Gini

*Gini coefficient*


---

### Description

Computes Gini coefficient of a given variable taking into account weights.

### Usage

```
Gini(X, W = rep(1, length(X)))
```

### Arguments

X is a data vector  
W is a vector of weights

### Details

Gini coefficient is given by:

$$G = \frac{\sum_{i=1}^n \sum_{j=1}^n |x_i - x_j|}{2n^2\bar{x}}$$

### Value

The value of Gini coefficient.

### References

Dixon P. M., Weiner, J., Mitchell-Olds, T., and Woodley, R.: (1987) Bootstrapping the Gini Coefficient of Inequality. *Ecology*, Volume 68 (5)

Firebaugh G.: (1999) Empirics of World Income Inequality, *American Journal of Sociology*

Deininger K.; Squire L.: (1996) A New Data Set Measuring Income Inequality, *The World Bank Economic Review*, Vol. 10, No. 3

### Examples

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Gini(X)
Gini(X,W)

data(Tourism)
```

```
#Gini coefficient for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Gini(X,W)
```

---

 Hoover

*Hoover index*


---

### Description

Computes Hoover inequality measure of a given variable taking into account weights.

### Usage

```
Hoover(X, W = rep(1, length(X)))
```

### Arguments

X is a data vector  
W is a vector of weights

### Details

Let  $x_i$  be the income of the  $i$ -th person and  $\bar{x}$  be the mean income. Then the Hoover index  $H$  is:

$$H = \frac{1}{2} \frac{\sum_i |x_i - \bar{x}|}{\sum_i x_i}$$

### Value

The value of Hoover coefficient.

### References

Hoover E. M. Jr.: (1936) The Measurement of Industrial Localization, The Review of Economics and Statistics, 18

Hoover E. M. Jr.: (1984) An Introduction to Regional Economics, ISBN 0-07-554440-7

### Examples

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Hoover(X)
Hoover(X,W)

data(Tourism)
```

```
#Hoover index for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Hoover(X,W)
```

---

ineq.weighted

*Weighted inequality measures*


---

### Description

Calculates weighted mean and sum of X (or median of X), and a set of relevant inequality measures.

### Usage

```
ineq.weighted(
  X,
  W = rep(1, length(X)),
  AF.norm = TRUE,
  Atkinson.e = 1,
  Jenkins.alfa = 0.8,
  Entropy.e = 0.5,
  Kolm.p = 1,
  Kolm.scale = "Standardization",
  Leti.norm = T,
  AN_Y.a = 1,
  AN_Y.b = 1,
  Apouey.a = 2/(1 - length(W[!is.na(W) & !is.na(X)])),
  Apouey.b = length(W[!is.na(W) & !is.na(X)])/(length(W[!is.na(W) & !is.na(X)] - 1),
  BL.withsqr = FALSE
)
```

### Arguments

X	is a data vector
W	is a vector of weights
AF.norm	(logical). If TRUE (default) then index is divided by its maximum possible value
Atkinson.e	is a parameter for Atkinson coefficient
Jenkins.alfa	is a parameter for Jenkins coefficient
Entropy.e	is a generalized entropy index parameter
Kolm.p	is a parameter for Kolm index
Kolm.scale	method of data standardization before computing
Leti.norm	(logical). If TRUE (default) then Leti index is divided by a maximum possible value

AN_Y.a	is a positive parameter for Abul Naga and Yalcin inequality measure
AN_Y.b	is a parameter for Abul Naga and Yalcin inequality measure
Apouey.a	is a parameter for Apouey inequality measure
Apouey.b	is a parameter for Apouey inequality measure
BL.withsqrt	if TRUE function returns index given by BL2, elsewhere by BL (default). See more in details of BL function.

### Details

Function checks if  $X$  is a numeric or an ordered factor. Then it calculates all appropriate inequality measures.

### Value

The data frame with weighted mean and sum of  $X$ , and all inequality measures relevant for a numeric data. In a case of an ordered factor, the data frame with median of  $X$ , and all relevant inequality measures.

### Examples

```
# Compare weighted and unweighted result.
X=1:10
W=1:10
ineq.weighted(X)
ineq.weighted(X,W)

data(Tourism)
# Results for Total expenditure with sample weights:
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
ineq.weighted(X)
ineq.weighted(X,W)
```

---

ineq.weighted.boot      *Weighted inequality measures with bootstrap*

---

### Description

For weighted mean and weighted total of  $X$  (or median of  $X$ ) as well as for each relevant inequality measure, returns outputs from ineq.weighted and bootstrap outcomes: expected value, bias (in %), standard deviation, coefficient of variation, lower and upper bound of confidence interval.

**Usage**

```

ineq.weighted.boot(
  X,
  W = rep(1, length(X)),
  B = 100,
  AF.norm = TRUE,
  Atkinson.e = 1,
  Jenkins.alfa = 0.8,
  Entropy.e = 0.5,
  Kolm.p = 1,
  Kolm.scale = "Standardization",
  Leti.norm = T,
  AN_Y.a = 1,
  AN_Y.b = 1,
  Apouey.a = 2/(1 - length(W[!is.na(W) & !is.na(X)])),
  Apouey.b = length(W[!is.na(W) & !is.na(X)])/(length(W[!is.na(W) & !is.na(X)] - 1),
  BL.withsqrt = FALSE,
  keepSamples = FALSE,
  keepMeasures = FALSE,
  conf.alpha = 0.05,
  calib.boot = FALSE,
  Xs = rep(1, length(X)),
  total = sum(W),
  calib.method = "truncated",
  bounds = c(low = 0, upp = 10)
)

```

**Arguments**

X	is a data vector
W	is a vector of weights
B	is a number of bootstrap samples.
AF.norm	(logical). If TRUE (default) then index is divided by its maximum possible value
Atkinson.e	is a parameter for Atkinson coefficient
Jenkins.alfa	is a parameter for Jenkins coefficient
Entropy.e	is a generalized entropy index parameter
Kolm.p	is a parameter for Kolm index
Kolm.scale	method of data standardization before computing
Leti.norm	(logical). If TRUE (default) then Leti index is divided by a maximum possible value
AN_Y.a	is a positive parameter for Abul Naga and Yalcin inequality measure
AN_Y.b	is a parameter for Abul Naga and Yalcin inequality measure
Apouey.a	is a parameter for Apouey inequality measure
Apouey.b	is a parameter for Apouey inequality measure

BL.withsqrt	if TRUE function returns index given by BL2, elsewhere by BL (default). See more in details of BL function.
keepSamples	if TRUE, it returns bootstrap samples of data (Xb) and weights (Wb)
keepMeasures	if TRUE, it returns values of all inequality measures for each bootstrap sample
conf.alpha	significance level for confidence interval
calib.boot	if FALSE, then naive bootstrap is performed, calibrated bootstrap elsewhere
Xs	matrix of calibration variables. By default it is a vector of 1's, applied if calib.boot is TRUE
total	vector of population totals. By default it is a sum of weights, applied if calib.boot is TRUE
calib.method	weights' calibration method for function calib (sampling)
bounds	vector of bounds for the g-weights used in the truncated and logit methods; 'low' is the smallest value and 'upp' is the largest value

## Details

By default, naive bootstrap is performed, that is no weights calibration is conducted. You can choose calibrated bootstrap to calibrate weights with respect to provided variables (Xs) and totals (total). Confidence interval is simply derived with quantile of order  $\alpha$  and  $1 - \alpha$  where  $\alpha$  is a significance level for confidence interval.

## Value

This functions returns a data frame from ineq.weighted extended with bootstrap results: expected value, bias (in %), standard deviation, coefficient of variation, lower and upper bound of confidence interval. If keepSamples=TRUE or keepMeasures==TRUE then the output becomes a list. If keepSamples=TRUE, the functions returns Xb and Wb, which are the samples of vector data and the samples of weights, respectively. If keepMeasures==TRUE, the functions returns Mb, which is a set of inequality measures from bootstrapping.

## Examples

```
# Inequality measures with additional statistics for numeric variable
X=1:10
W=1:10
ineq.weighted.boot(X,W,B=10)

# Inequality measures with additional statistics for ordered factor variable
X=factor(c('H', 'H', 'M', 'M', 'L', 'L'),levels = c('L', 'M', 'H'),ordered = TRUE)
W=c(2,2,3,3,8,8)
ineq.weighted.boot(X,W,B=10)
```

---

 Jenkins

*Jenkins, Cowell and Flachaire*


---

**Description**

Computes Jenkins as well as Cowell and Flachaire inequality measure of a given variable taking into account weights.

**Usage**

```
Jenkins(X, W = rep(1, length(X)), alfa = 0.8)
```

**Arguments**

X	is a data vector
W	is a vector of weights
alfa	is the Jenkins coefficient parameter

**Details**

Jenkins coefficient is given by:

$$J = 1 - \sum_{j=0}^{K-1} (p_{j+1} - p_j)(GL_j + GL_{j+1})$$

where GL is Generalized Lorenz curve.

Cowell and Flachaire coefficient with alpha parameter is given by:

$$I(\alpha) = \frac{1}{\alpha(\alpha - 1)} \left( \frac{1}{N} \sum_{i=1}^N s_i^\alpha - 1 \right)$$

for  $\alpha \in (0, 1)$ , and

$$I(0) = -\frac{1}{N} \sum_{i=1}^N \log(s_i)$$

for  $\alpha = 0$ .

**Value**

The value of Jenkins, Cowell and Flachaire coefficient.

**References**

- Jenkins S. P. and P. J. Lambert: (1997) Three 'I's of Poverty Curves, with an Analysis of U.K. Poverty Trends
- Cowell F. A.: (2000) Measurement of Inequality, Handbook of Income Distribution
- Cowell F. A., Flachaire E.: (2017) Inequality with Ordinal Data



**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Jenkins(X)
Jenkins(X,W)

data(Tourism)
#Jenkins, Cowell and Flachaire coefficients for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Jenkins(X,W)
```

---

Kolm

*Kolm index*


---

**Description**

Computes Kolm inequality measure of a given variable taking into account weights.

**Usage**

```
Kolm(X, W = rep(1, length(X)), parameter = 1, scale = "None")
```

**Arguments**

X	is a data vector
W	is a vector of weights
parameter	is a Kolm parameter
scale	method of data scaling (None, Normalization, Unitarization, Standardization)

**Details**

Kolm index with parameter  $\alpha$  is defined as:

$$K = \frac{1}{\alpha} (\log(\sum_{i=1}^n \exp(\alpha(w_i - \mu))) - \log(n))$$

Kolm index is scale-dependent. Basic normalization methods can be applied before final computation.

**Value**

The value of Kolm coefficient.

## References

- Kolm S. C.: (1976) Unequal inequalities I and II  
 Kolm S. C.: (1996) Intermediate measures of inequality  
 Chakravarty S. R.: (2009) Inequality, Polarization and Poverty e-ISBN 978-0-387-79253-8

## Examples

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Kolm(X)
Kolm(X,W)

# Compare raw and standardized data.
Kolm(X,W)
Kolm(X,W, scale ="Standardization")

# Changing units has an impact on the final result
Kolm(X)
Kolm(10*X)

# Changing units has no impact on the final result with standardized data
Kolm(X,scale ="Standardization")
Kolm(10*X,scale ="Standardization")
```

---

Leti

*Leti index*

---

## Description

Computes Leti inequality measure of a given variable taking into account weights.

## Usage

```
Leti(X, W = rep(1, length(X)), norm = T)
```

## Arguments

X	is a data vector (ordered factor or numeric)
W	is a vector of weights
norm	(logical). If TRUE (default) then Leti index is divided by a maximum possible value which is $(k - 1)/2$ where $k$ is a number of categories.

**Details**

Let  $n_i$  be the number of individuals in category  $i$  and let  $N$  be the total sample size. Cumulative distribution is given by  $F_i = \frac{\sum_{j=1}^i n_j}{N}$ . Leti index is defined as:

$$L = 2 \sum_{i=1}^{k-1} F_i(1 - F_i)$$

**Value**

The value of Leti coefficient.

**References**

Leti G.: (1983). Statistica descrittiva, il Mulino, Bologna. ISBN: 8-8150-0278-2

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Leti(X)
Leti(X,W)

data(Tourism)
#Leti index for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Leti(X,W)
```

---

medianf

*Median of ordered factor or numeric*

---

**Description**

Computes median of ordered factor or numeric variable taking into account weights.

**Usage**

```
medianf(X, W = rep(1, length(X)))
```

**Arguments**

X is a data vector (numeric or ordered factor)  
W is a vector of weights

**Details**

Calculates median based on cumulative distribution. Tailored for ordered factors.

**Value**

The median category (number or label) of ordered factor.

**Examples**

```
# Compare weighted and unweighted result
X=factor(c('H', 'H', 'M', 'M', 'L', 'L'), levels = c('L', 'M', 'H'), ordered = TRUE)
W=c(2,2,3,3,8,8)
medianf(X)
medianf(X,W)
```

---

Palma

*Palma index*

---

**Description**

Palma proportion - originally the ratio of the total income of the 10% richest people to the 40% poorest people.

**Usage**

```
Palma(X, W = rep(1, length(X)))
```

**Arguments**

X is a data vector (numeric or ordered factor)  
 W is a vector of weights

**Details**

Palma index is calculated by the following formula:

$$Palma = \frac{H}{L}$$

where  $H$  is share of 10% of the highest values,  $L$  is share of 40% of the lowest values.

**Value**

The value of Palma coefficient.

## References

Cobham A., Sumner A.: (2013) Putting the Gini Back in the Bottle? 'The Palma' as a Policy-Relevant Measure of Inequality

Palma J. G.: (2011) Homogeneous middles vs. heterogeneous tails, and the end of the 'Inverted-U': the share of the rich is what it's all about

## Examples

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Palma(X)
Palma(X,W)

data(Tourism)
#Palma index for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Palma(X,W)
```

---

Prop20\_20

*Proportion 20:20*

---

## Description

20:20 ratio - originally the ratio of the total income of the 20% richest people to the 20% poorest people.

## Usage

```
Prop20_20(X, W = rep(1, length(X)))
```

## Arguments

X is a data vector (numeric or ordered factor)  
 W is a vector of weights

## Details

20:20 ratio is calculated as follows:

$$Prop = \frac{H}{L}$$

where  $H$  is share of 20% of the highest values,  $L$  is share of 20% of the lowest values.

**Value**

The value of 20:20 ratio coefficient.

**References**

Panel Data Econometrics: Theoretical Contributions And Empirical Applications edited by Badi Hani Baltag

Notes on Statistical Sources and Methods - The Equality Trust.

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Prop20_20(X)
Prop20_20(X,W)

data(Tourism)
#Prop20_20 proportion for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Prop20_20(X,W)
```

---

 RicciSchutz

*Ricci and Schutz index*


---

**Description**

Computes Ricci and Schutz inequality measure of a given variable taking into account weights.

**Usage**

```
RicciSchutz(X, W = rep(1, length(X)))
```

**Arguments**

X	is a data vector
W	is a vector of weights

**Details**

In the case of an empirical distribution with n elements where  $y_i$  denotes the wealth of household i and  $\bar{y}$  the sample average, the Ricci and Schutz coefficient can be expressed as:

$$RS = \frac{1}{2n} \sum_{i=1}^n \frac{|y_i - \bar{y}|}{\bar{y}}$$

**Value**

The value of Ricci and Schutz coefficient.

**References**

Coulter P. B.: (1989) Measuring Inequality ISBN 0-8133-7726-9

Eliazar I. I., Sokolov I. M.: (2010) Measuring statistical heterogeneity: The Pietra index

Costa R. N., Pérez-Duarte S.: (2019) Not all inequality measures were created equal, Statistics Paper Series, No 31

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
RicciSchutz(X)
RicciSchutz(X,W)

data(Tourism)
#Ricci and Schutz index for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
RicciSchutz(X,W)
```

---

Theil\_L

*Theil L*


---

**Description**

Computes Theil\_L inequality measure of a given variable taking into account weights.

**Usage**

```
Theil_L(X, W = rep(1, length(X)))
```

**Arguments**

X is a data vector

W is a vector of weights

**Details**

Theil L index is defined as:

$$T_L = T_{\alpha=0} = \frac{1}{N} \sum_{i=1}^N \ln\left(\frac{\mu}{x_i}\right)$$

where

$$\mu = \frac{1}{N} \sum_{i=1}^N x_i$$

**Value**

The value of Theil\_L coefficient.

**References**

Serebrenik A., van den Brand M.: Theil index for aggregation of software metrics values. 26th IEEE International Conference on Software Maintenance. IEEE Computer Society.

Conceição P., Ferreira P.: (2000) The Young Person's Guide to the Theil Index: Suggesting Intuitive Interpretations and Exploring Analytical Applications

OECD: (2020) Regions and Cities at a Glance 2020, Chapter: Indexes and estimation techniques

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Theil_L(X)
Theil_L(X,W)

data(Tourism)
# Theil L coefficient for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Theil_L(X,W)
```

---

Theil\_T

*Theil T*


---

**Description**

Computes Theil\_T inequality measure of a given variable taking into account weights.

**Usage**

```
Theil_T(X, W = rep(1, length(X)))
```



**Arguments**

X is a data vector  
 W is a vector of weights

**Details**

Theil T index is defined as:

$$T_T = T_{\alpha=1} = \frac{1}{N} \sum_{i=1}^N \frac{x_i}{\mu} \ln\left(\frac{x_i}{\mu}\right)$$

where

$$\mu = \frac{1}{N} \sum_{i=1}^N x_i$$

**Value**

The value of Theil\_T coefficient.

**References**

Serebrenik A., van den Brand M.: Theil index for aggregation of software metrics values. 26th IEEE International Conference on Software Maintenance. IEEE Computer Society.

Conceição P., Ferreira P.: (2000) The Young Person's Guide to the Theil Index: Suggesting Intuitive Interpretations and Exploring Analytical Applications

OECD: (2020) Regions and Cities at a Glance 2020, Chapter: Indexes and estimation techniques

**Examples**

```
# Compare weighted and unweighted result
X=1:10
W=1:10
Theil_T(X)
Theil_T(X,W)

data(Tourism)
# Theil T coefficient for Total expenditure with sample weights
X=Tourism$`Total expenditure`
W=Tourism$`Sample weight`
Theil_T(X,W)
```

---

Tourism

*Sample survey on trips*

---

**Description**

Data from sample survey on trips conducted in Polish households.

**Usage**

```
data(Tourism)
```

**Format**

A data frame with 384 observations of 14 variables

- Year
- Group of countries
- Purpose of trip
- Accommodation type
- Total expenditure
- Expenditure for organiser
- Private expenditure
- Expenditure on accommodation
- Expenditure on restaurants & café
- Expenditure on transport
- Expenditure on commodities
- Number of trip's participants
- Nights spent
- Sample weight

**Details**

Answers were modified due to disclosure control. Data presents only part of full database.

---

Well\_being

*Sample survey on quality of life*

---

**Description**

Data from sample survey on quality of life conducted on Polish-Ukrainian border in 2015 and 2019.

**Usage**

```
data(Well_being)
```

**Format**

A data frame with 1197 observations of 27 variables

- Area. Rural and urban
- Gender. Male and female
- Year. Year of survey (2015 and 2019)
- V1. I have good opportunities to use my talents and skills at work
- V2. I am treated with respect by others at work
- V3. I have adequate opportunities for vacations or leisure activities
- V4. The quality of local services where (I) live is good
- V5. There is very little pollution from cars or other sources where I spend most of my time
- V6. There are parks and green areas near my residence
- V7. I have the freedom to plan my life the way I want to
- V8. I feel safe walking around my neighborhood during the day
- V9. Overall, to what extent are you currently satisfied with your life
- V10. Overall, to what extent do you feel that the things you do in life are worthwhile
- V11. How do you rate your health
- V12. How do you rate your work
- V13. How do you rate your sleep
- V14. How do you rate your leisure time
- V15. How do you rate your family life
- V16. How do you rate your community and public affairs life
- V17. How do you rate your personal plans
- V18. How do you rate your housing conditions
- V19. How do you rate your personal income
- V20. How do you rate your personal prospects
- V21. Does being part of the local community make you feel good about yourself
- V22. Do you have a say in what the local community is like
- V23. Is your neighborhood a good place for you to live
- Weight. Sample weight for each household

**Details**

Questions are on Likert scale: 1 - the worst assessment, 5 - the best assessment. Only 23 question were selected out of over 100 questions. Answers were modified due to disclosure control.

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